

THE ALGORITHM

The gradient of $F_{DV}^{(L)}$ with respect to $\vec{\psi}$ @ fixed q is

$$\nabla_{\vec{\psi}} \mathbf{P}^{(L)} = -\nabla_{\vec{\psi}} \mathbf{RL}^{(L)} \cdot (-\mathbf{c}^{(L)}) - \mathbf{RL}^{(L)} \cdot (-\nabla_{\vec{\psi}} \mathbf{c}^{(L)}) + \nabla_{\vec{\psi}} \vec{\beta}^{(L)}$$

where

$$\mathbf{P}^{(L)} \cdot (-\nabla_{\vec{\psi}} \mathbf{c}^{(L)}) = \nabla_{\vec{\psi}} \mathbf{P}^{(L)} \cdot (-\mathbf{c}^{(L)}) - \nabla_{\vec{\psi}} \mathbf{g}^{(L)}.$$

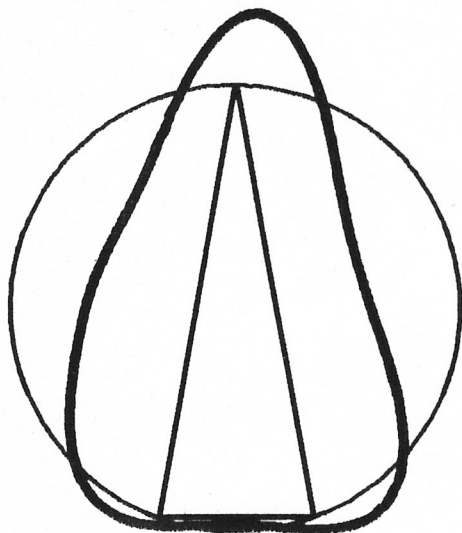
FEATURES

- 1) ♦ The scattering data are $\{A[\mathbf{k}_q; \phi_j; \gamma_q], j \in N_q, q \in Q\}$.
- 2) ♦ Superposition of limited aperture – multiple views allowed.
- 3) ♦ The cost function to be minimized is $F_{DV}^{(L)}[\vec{\psi}, \vec{\gamma}]$.
- 4) ♦ The unknowns are $\vec{\psi} \in \Psi_{\text{adm}}$ and $\vec{\gamma} \in ([0, 2\pi])^{\text{card}[Q]}$.
- 5) The DIRICHLET BC and the boundary to far zone relation are represented by approximate forward propagation.
- 6) $\mathbf{P}_q^{(L)}, \mathbf{RL}_q^{(L)}$ depend on $\vec{\psi}$ and on k_q (not on $\mathbf{k}_q$).
- 7) $\{\vec{\beta}_q^{(L)}\}$ and $\{\mathbf{g}_q^{(L)}\}$ depend on $\vec{\psi}$ and on $\mathbf{k}_q$.
- 8) ♦ Only $\mathbf{P}_q^{(L)}$ has to be inverted; $[\mathbf{P}_q^{(L)}]^{-1} \exists$ unconditionally.

NUMERICAL RESULTS FROM $F_{DV}^{(L)}$ MINIMIZATION

Ipswich files *ips009/ips009FV**

Full aperture data obtained via reciprocity of $A[\mathbf{k}_q; \phi_j; \gamma_q]$

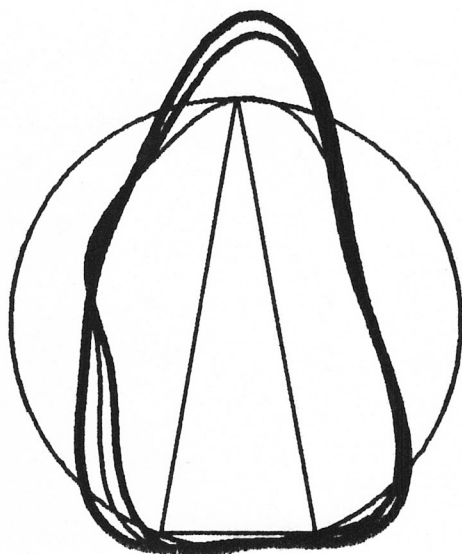


$$\{\mathbf{k}_q, 1 \leq q \leq 4\}$$

$$L = 12, I = 10$$

$$\frac{\psi_4^{(0)}}{\psi_1^{(0)}} = -0.4$$

MF9x4CA $r_0 = .495868\text{D} + 01$ It. = 15
 $B^{[12]} = .425680\text{D} + 03; \|\nabla B\| = .258242\text{D} + 05$

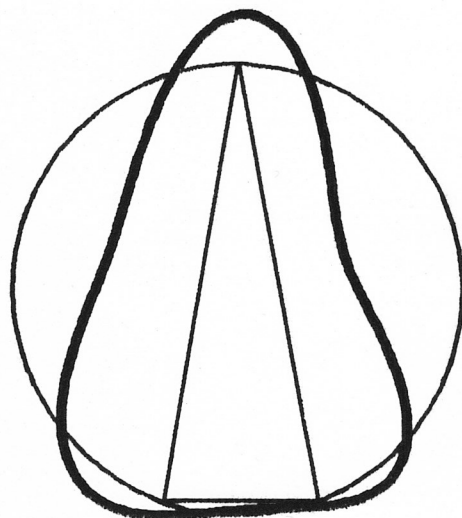


$$\{\mathbf{k}_q, 1 \leq q \leq 5\}$$

$$L = 12, I = 10$$

$$\frac{\psi_4^{(0)}}{\psi_1^{(0)}} = -0.4$$

MF9x5CA $r_0 = .495868\text{D} + 01$ It. = 15
 $B^{[12]} = .485822\text{D} + 03; \|\nabla B\| = .195682\text{D} + 05$
MF9x5CA $r_0 = .409808\text{D} + 01$ It. = 15
 $B^{[12]} = .494881\text{D} + 03; \|\nabla B\| = .177667\text{D} + 05$
MF9x5CA $r_0 = .450789\text{D} + 01$ It. = 15
 $B^{[12]} = .514020\text{D} + 03; \|\nabla B\| = .195457\text{D} + 05$



$$\{\mathbf{k}_q, 1 \leq q \leq 5\}$$

$$L = 14, I = 10$$

$$\frac{\psi_4^{(0)}}{\psi_1^{(0)}} = -0.4$$

MF9x5EA $r_0 = .495868\text{D} + 01$ It. = 15
 $B^{[14]} = .464231\text{D} + 03; \|\nabla B\| = .537194\text{D} + 05$

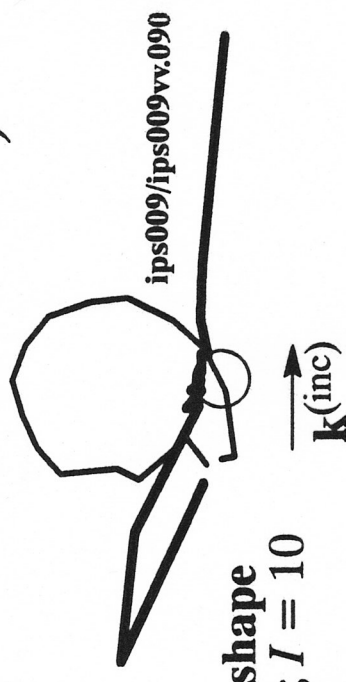
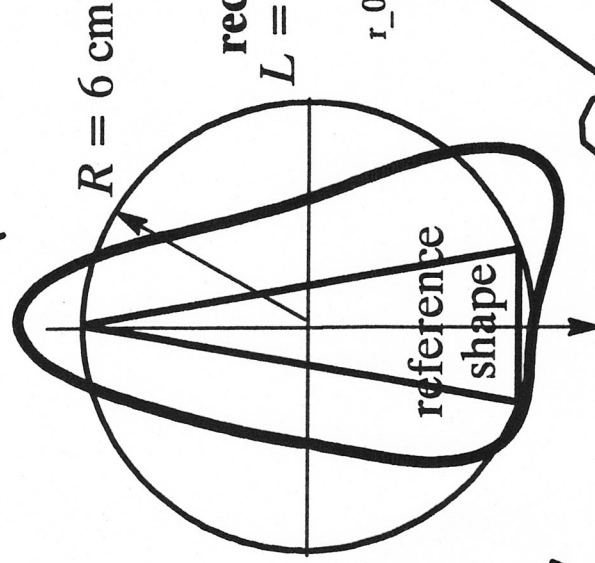
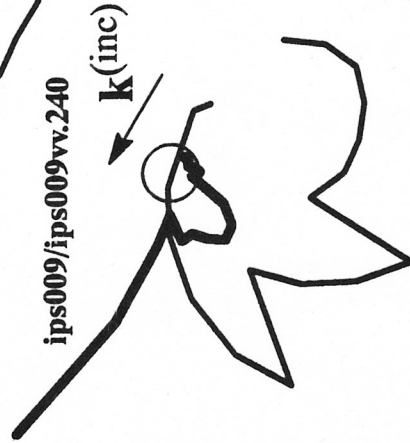
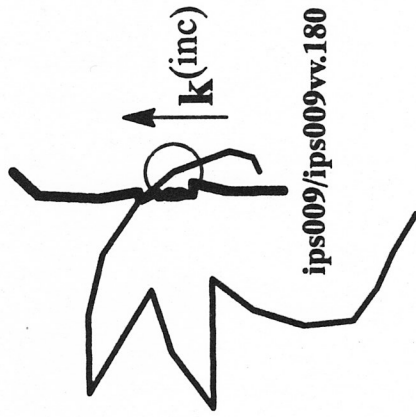
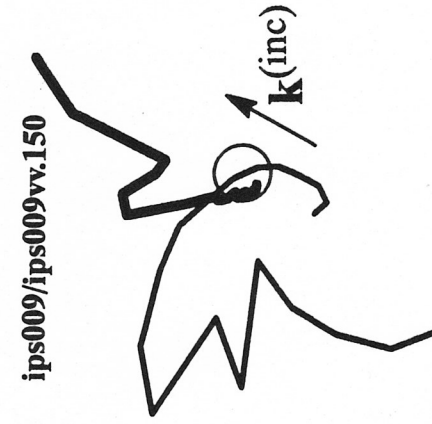
RECONSTRUCTION

BY F_{DV}

MINIMIZATION AND LIMITED APERTURE

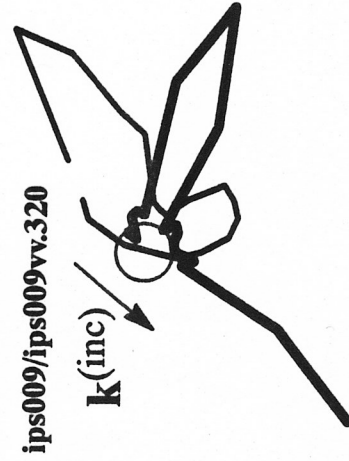
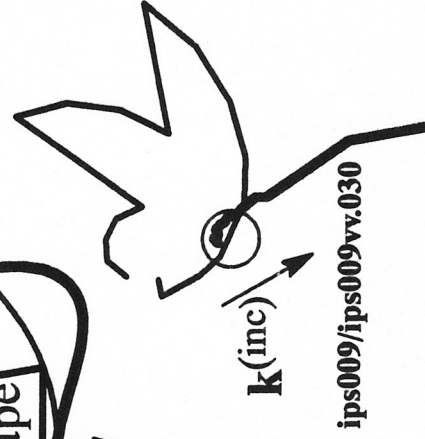
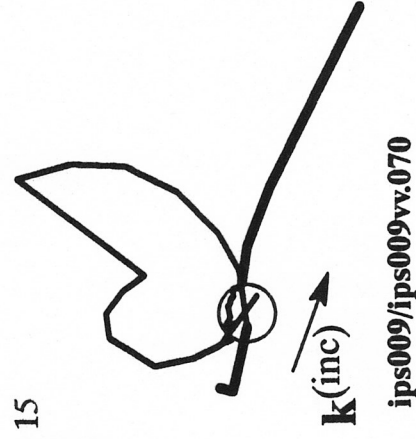
IPSWICH DATA

(π rad for each view)



reconstructed shape
 $L = 12; n_p = 63; I = 10$
Mr9x7CA

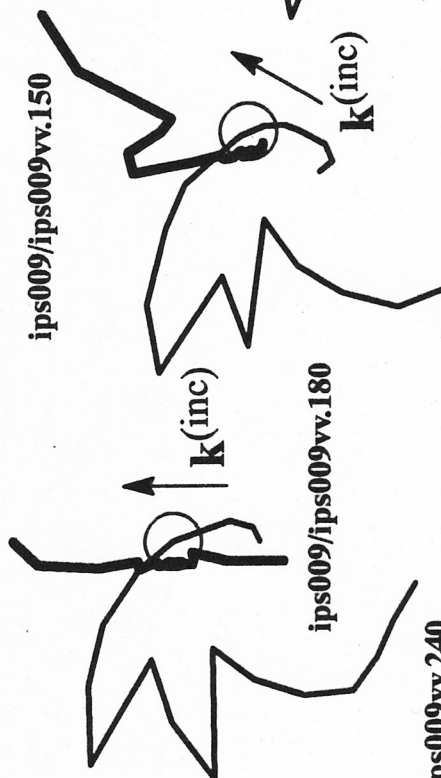
$r_0 = .409808D+01; It. = 15$
 $B^{[12]} = .325603D+03$
 $\|\nabla B\| = .109153D+05$



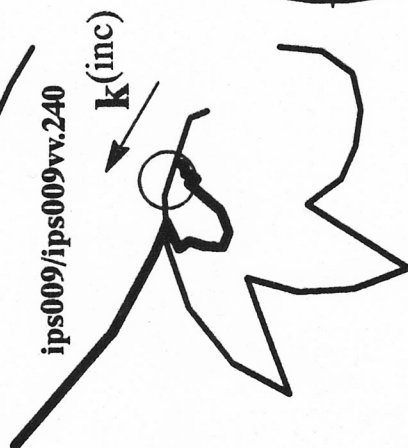
RECONSTRUCTION BY F_{DV} MINIMIZATION

AND LIMITED APERTURE IPSWICH DATA

(π rad for each view)

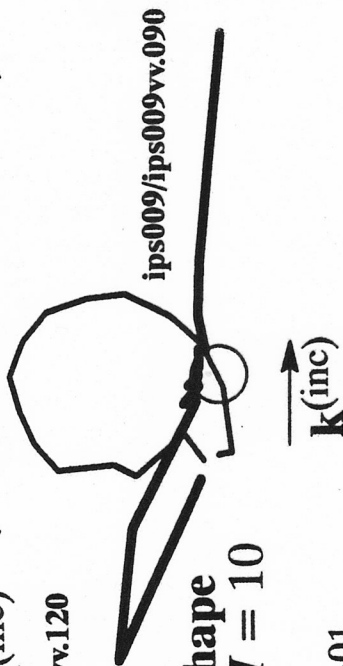


ips009/ips009vv.180



$R = 6 \text{ cm}$

ips009/ips009vv.120



reconstructed shape
 $L = 12; n_p = 63; I = 10$

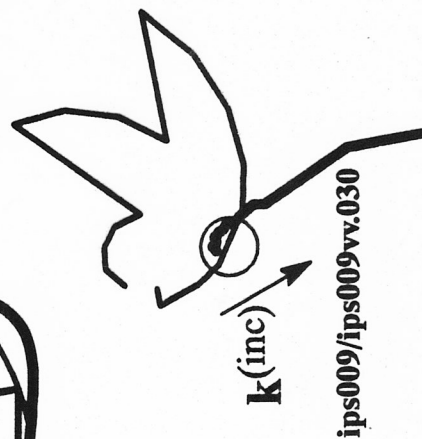
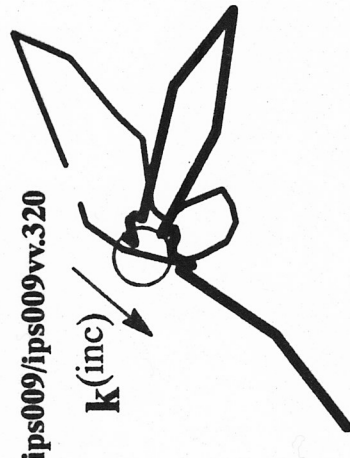
Mr9x8CA

$r_0 = .409808D+01$

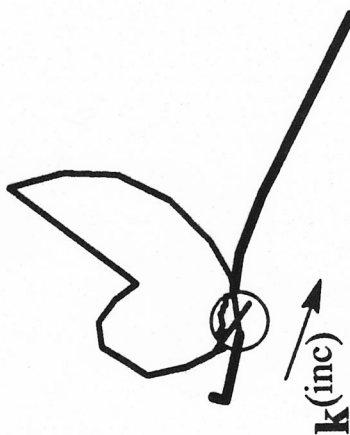
$It = 15$

$B^{[12]} = .449799D+03$

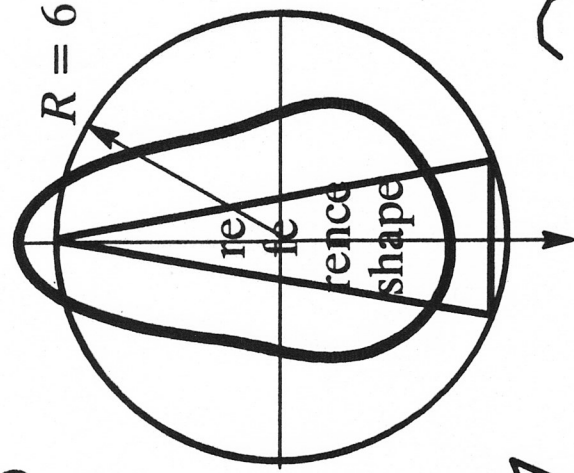
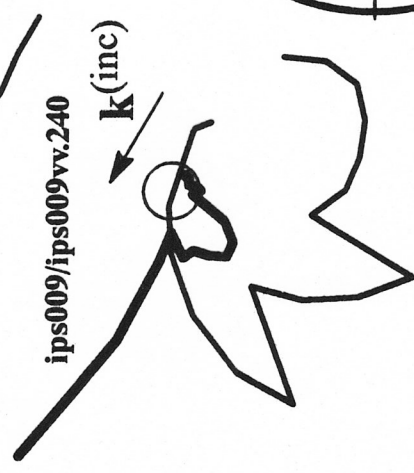
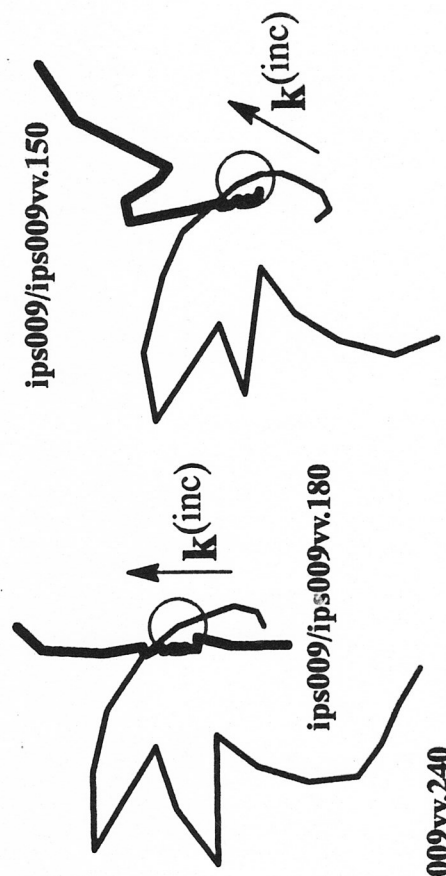
$\|\nabla B\| = .172676D+05$



ips009/ips009vv.070



RECONSTRUCTION BY F_{DV} MINIMIZATION AND LIMITED APERTURE IPSWICH DATA (π rad for each view)



reconstructed shape
 $L = 14; n_p = 63; I = 10$
Mr9x7EA

$r_0 = .409808D+01$
 $It = 10$
 $B^{[14]} = .385652D+03$
 $\|\nabla B\| = .357053D+06$

